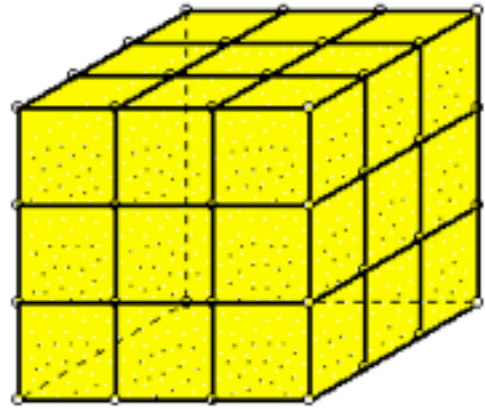


Painted Cubes

PART A: A white $3 \times 3 \times 3$ cube is built using smaller $1 \times 1 \times 1$ cubes. If this big cube is dipped in yellow paint, then taken apart into small cubes again, how many of the original, individual cubes will have...

1. NO sides painted yellow?
2. ONE side painted yellow?
3. TWO sides painted yellow?
4. THREE sides painted yellow?
5. More than three sides painted yellow?



PART B: Come up with a rule for knowing how many individual cubes are painted in some way in an $N \times N \times N$ cube. Your rule should help someone predict how many cubes will have 0 sides painted, 1 side painted, 2 sides painted, 3 sides painted and more than 3 sides painted.